

1. (1) $\text{Na}(s) + \frac{1}{2}\text{Cl}_2(g) \rightarrow \text{Na}(g) + \text{Cl}(g); \Delta H = +230 \text{ kJ}$
 (2) $\text{Na}(g) + \text{Cl}(g) \rightarrow \text{Na}^+(g) + \text{Cl}^-(g); \Delta H = +147 \text{ kJ}$
 (3) $\text{Na}(s) + \frac{1}{2}\text{Cl}_2(g) \rightarrow \text{NaCl}(s); \Delta H = -411 \text{ kJ}$
 need $\text{Na}^+(g)$ and $\text{Cl}^-(g)$ on the LHS; reverse (2) \rightarrow (4)
 need $\text{NaCl}(s)$ on the RHS; use (3) as is
 need $\text{Na}(g)$ and $\text{Cl}(g)$ on the LHS to cancel $\text{Na}(g)$ and $\text{Cl}(g)$ on the RHS in (4); reverse (1) \rightarrow (5)
 (4) $\text{Na}^+(g) + \text{Cl}^-(g) \rightarrow \text{Na}(g) + \text{Cl}(g); \Delta H = -147 \text{ kJ}$
 (3) $\text{Na}(s) + \frac{1}{2}\text{Cl}_2(g) \rightarrow \text{NaCl}(s); \Delta H = -411 \text{ kJ}$
 (5) $\text{Na}(g) + \text{Cl}(g) \rightarrow \text{Na}(s) + \frac{1}{2}\text{Cl}_2(g); \Delta H = -230 \text{ kJ}$
 adding (4)+(3)+(5) gives $\text{Na}^+(g) + \text{Cl}^-(g) \rightarrow \text{NaCl}(s); \Delta H = -788 \text{ kJ}$

2. ΔH_f^0 of $\text{VCl}_3(s)$ is ΔH for $\text{V}(s) + 1.5\text{Cl}_2(g) \rightarrow \text{VCl}_3(s)$
 (1) $\text{V}(s) + 2\text{Cl}_2(g) \rightarrow \text{VCl}_4(l); \Delta H = -569.4 \text{ kJ}$
 (2) $\text{VCl}_3(s) \rightarrow \text{VCl}_2(s) + \frac{1}{2}\text{Cl}_2(g); \Delta H = +128.9 \text{ kJ}$
 (3) $2\text{VCl}_3(s) \rightarrow \text{VCl}_2(s) + \text{VCl}_4(l); \Delta H = +140.2 \text{ kJ}$
 need $\text{V}(s)$ on the LHS; use (1) as is
 need $\text{VCl}_4(l)$ on the LHS to cancel $\text{VCl}_4(l)$ on the RHS in (1); reverse (3) \rightarrow (4)
 need $\text{VCl}_2(s)$ on the RHS to cancel $\text{VCl}_2(s)$ on the LHS in (4); use (2) as is
 (1) $\text{V}(s) + 2\text{Cl}_2(g) \rightarrow \text{VCl}_4(l); \Delta H = -569.4 \text{ kJ}$
 (4) $\text{VCl}_2(s) + \text{VCl}_4(l) \rightarrow 2\text{VCl}_3(s); \Delta H = -140.2 \text{ kJ}$
 (2) $\text{VCl}_3(s) \rightarrow \text{VCl}_2(s) + \frac{1}{2}\text{Cl}_2(g); \Delta H = +128.9 \text{ kJ}$
 adding (1)+(4)+(2) gives $\text{V}(s) + 1.5\text{Cl}_2(g) \rightarrow \text{VCl}_3(s); \Delta H = -580.7 \text{ kJ}$

3. (1) $2\text{Al}_2\text{O}_3(s) \rightarrow 4\text{Al}(s) + 3\text{O}_2(g); \Delta H = +3340 \text{ kJ}$
 (a) ΔH_f^0 for $\text{Al}_2\text{O}_3(s)$ is ΔH for
 (2) $2\text{Al}(s) + 1.5\text{O}_2(g) \rightarrow \text{Al}_2\text{O}_3(s)$
 but (2) is (1) divided by 2 and reversed
 hence ΔH_f^0 for $\text{Al}_2\text{O}_3(s)$ is $-3340 \text{ kJ}/2 = -1670 \text{ kJ}$

$$(b) \quad 10.0 \text{ g Al}_2\text{O}_3 \times \frac{1 \text{ mol Al}_2\text{O}_3}{102 \text{ g Al}_2\text{O}_3} \times \frac{3340 \text{ kJ}}{2 \text{ mol Al}_2\text{O}_3} = 164 \text{ kJ}$$

4. $\Delta T = (25.00 - 21.18)^\circ\text{C} = 3.82^\circ\text{C}$
 $Q = \text{heat lost by } 50.0 \text{ g water} + \text{heat lost by calorimeter}$
 $(50.0 \text{ g} \times 4.18 \text{ J/g}\cdot^\circ\text{C} \times 3.82^\circ\text{C}) + (75.0 \text{ J/}^\circ\text{C} \times 3.92^\circ\text{C}) = 1085 \text{ J}$
 since the temperature decreased, ΔH for the process
 $\text{KClO}_3(s) \rightarrow \text{K}^+(aq) + \text{ClO}_3^-(aq)$ is $+ Q/\text{mol KClO}_3$

$$Q/\text{mol KClO}_3 = \frac{1085 \text{ J}}{3.17 \text{ g}} \times \frac{122.6 \text{ g}}{1 \text{ mol}} = 42.0 \text{ kJ/mol}$$

$$\Delta H = +42.0 \text{ kJ}$$

$$5. \quad \text{heat given off} = 2.48 \text{ g Cu} \times \frac{128.4 \text{ kJ}}{63.55 \text{ g Cu}} = 5.01 \text{ kJ}$$

$$Q = 5.01 \times 10^3 \text{ J} = (125 \text{ g} \times 4.18 \text{ J/g}\cdot^\circ\text{C} \times \Delta T) + (75.0 \text{ J/}^\circ\text{C} \times \Delta T)$$

$$5.01 \times 10^3 \text{ J} = (522.5 + 75.0) \Delta T = 597.5 \Delta T$$

$$\Delta T = \frac{5.01 \times 10^3}{597.5} = 8.38^\circ\text{C}$$

since the reaction is exothermic, $T_{\text{final}} = (22.50 + 8.38) = 30.88^\circ\text{C}$

$$6. \quad \Delta T = (25.54 - 24.00)^\circ\text{C} = 1.54^\circ\text{C}. \text{ Total volume} = (155 + 260) \text{ mL} = 415 \text{ mL}$$

Assuming density = 1.00 g/mL, total mass = 415 g

$$Q = (415 \text{ g} \times 4.184 \text{ J/g}\cdot^\circ\text{C} \times 1.54^\circ\text{C}) + (40.4 \text{ J/}^\circ\text{C} \times 1.54^\circ\text{C})$$

$$= 2736 \text{ J} = 2.736 \text{ kJ}$$

$$\text{mol H}_3\text{PO}_4 = 0.155 \text{ L} \times 0.1250 \text{ M} = 0.01938$$

$$\text{mol Sr(OH)}_2 = 0.260 \text{ L} \times 0.1000 \text{ M} = 0.02600$$

$$0.01938 \text{ mol H}_3\text{PO}_4 \text{ needs } 0.01938 \text{ mol H}_3\text{PO}_4 \times \frac{3 \text{ mol Sr(OH)}_2}{2 \text{ mol H}_3\text{PO}_4}$$

$$= 0.02907 \text{ mol Sr(OH)}_2$$

Therefore, Sr(OH)_2 is the limiting reactant

$$\frac{Q}{\text{mol Sr(OH)}_2} = \frac{2.736 \text{ kJ}}{0.0260} = 105.2 \text{ kJ}$$

$$\Delta H = -Q \text{ for 3 moles of Sr(OH)}_2; \Delta H = -(105.2 \times 3) = -316 \text{ kJ}$$

$$7. \quad \Delta T = (25.64 - 23.40)^\circ\text{C} = 2.24^\circ\text{C}$$

heat gained on 6.00 kg H_2O increasing in temperature by 2.24°C

$$= 6.00 \times 10^3 \text{ g} \times 4.184 \text{ J/g}\cdot^\circ\text{C} \times 2.24^\circ\text{C} = 5.623 \times 10^4 \text{ J} = 56.23 \text{ kJ}$$

heat gained by calorimeter increasing in temperature by 2.24°C

$$= 3.180 \text{ kJ/}^\circ\text{C} \times 2.24^\circ\text{C} = 7.12 \text{ kJ}$$

total heat gained = 63.35 kJ = heat given off in the reaction

$$Q/\text{mol C}_{12}\text{H}_{22}\text{O}_{11} = \frac{63.35 \text{ kJ}}{3.85 \text{ g}} \times \frac{342.2 \text{ g}}{1 \text{ mol}} = 5.631 \times 10^3 \text{ kJ}$$

since the reaction gave off heat, $\Delta H = -5.631 \times 10^3 \text{ kJ}$ and the reaction is



$$\Delta H = \sum \Delta H_f^0 \text{ products} - \sum \Delta H_f^0 \text{ reactants}$$

$$-5631 = [12(-393.5) + 11(-285.8)] - \Delta H_f^0 \text{ sucrose}$$

$$\Delta H_f^0 \text{ sucrose} = -4722 + (-3144) + 5631 = -2235 \text{ kJ}$$

8. let ΔT = change in temperature
 heat gained by 5.00 kg water increasing in temperature by ΔT
 $= 5.00 \times 10^3 \text{ g} \times 4.18 \text{ J/g}\cdot^\circ\text{C} \times \Delta T = 20.9 \Delta T \times 10^3 \text{ J} = 20.9 \Delta T \text{ kJ}$
 heat gained by calorimeter increasing in temperature by ΔT
 $= 3.612 \text{ kJ}/^\circ\text{C} \times \Delta T = 3.612 \Delta T \text{ kJ}$
 since heat given off = 69.3 kJ, $(20.9 + 3.612)\Delta T = 69.3$
 $24.51 \Delta T = 69.3 \quad \Delta T = 69.3/24.51 = 2.83^\circ\text{C}$
 Final temperature = $(23.00 + 2.83)^\circ\text{C} = 25.83^\circ\text{C}$

9. $\Delta H_f \text{ HI}(g) = 25.9 \text{ kJ/mole}$
 (1) $\frac{1}{2}\text{H}_2(g) + \frac{1}{2}\text{I}_2(s) \rightarrow \text{HI}(g); \Delta H = 25.9 \text{ kJ}$
 ΔH of sublimation of $\text{I}_2 = 62.4 \text{ kJ/mole}$
 (2) $\text{I}_2(s) \rightarrow \text{I}_2(g); \Delta H = 62.4 \text{ kJ}$
 (3) $\text{I}_2(g) \rightarrow \text{I}_2(s); \Delta H = -62.4 \text{ kJ}$
 (4) $\frac{1}{2}\text{I}_2(g) \rightarrow \frac{1}{2}\text{I}_2(s); \Delta H = -31.2 \text{ kJ}$
 (1) + (4) gives:
 $\frac{1}{2}\text{H}_2(g) + \frac{1}{2}\text{I}_2(g) \rightarrow \text{HI}(g); \Delta H = (25.9 - 31.2) \text{ kJ} = -5.3 \text{ kJ}$

10. Let final temperature = T

$$\text{Heat gained on melting} = 125 \text{ g} \times \frac{1 \text{ mol}}{60.0 \text{ g}} \times \frac{11.7 \text{ kJ}}{1 \text{ mol}} = 24.38 \text{ kJ}$$

Heat gained on warming from 16.7°C to T:

$$= 125 \text{ g} \times \frac{1 \text{ mol}}{60.0 \text{ g}} \times \frac{0.125 \text{ kJ}}{^\circ\text{C}\cdot\text{mol}} \times (T - 16.7)^\circ\text{C}$$

$$= (0.2604 T - 4.349) \text{ kJ}$$

Heat lost on cooling from 33.8°C to T:

$$= 755 \text{ g} \times \frac{1 \text{ mol}}{60.0 \text{ g}} \times \frac{0.125 \text{ kJ}}{^\circ\text{C}\cdot\text{mol}} \times (33.8 - T)^\circ\text{C}$$

$$= (53.16 - 1.573 T) \text{ kJ}$$

Heat gained = heat lost

$$0.2604 T - 4.349 + 24.38 = 53.16 - 1.573 T$$

$$(0.2604 + 1.573)T = 53.16 + 4.349 - 24.38$$

$$1.833 T = 33.129$$

$$T = 18.1^\circ\text{C}$$

CHECK:

$$24.38 + \left[\frac{125}{60} \times 0.125 \times (18.1 - 16.7) \right] = \frac{775}{60} \times 0.125 \times (33.8 - 18.1)$$

$$24.7 = 24.7$$

11. (a) From Appendix C: $\Delta H_f^0 \text{Al}_2\text{O}_3 = -1676 \text{ kJ}$; $\Delta H_f^0 \text{Fe}_2\text{O}_3 = -825.5 \text{ kJ}$
for the reaction, $\Delta H = \Delta H_f^0 \text{Al}_2\text{O}_3 - \Delta H_f^0 \text{Fe}_2\text{O}_3 = [-1676 - (-825.5)] \text{ kJ}$
 $= -850.5 \text{ kJ}$
- (b) For the reaction as written, 1 mol Al_2O_3 (102 g) and 2 mol Fe (111.7 g) are formed when 850.5 kJ of heat are evolved. Since these are the only materials present, Q (the heat evolved, 850.5 kJ) must be equal to the sum of (mass x specific heat x ΔT) for the Al_2O_3 and Fe.
 $850.5 \times 10^3 \text{ J} = 102 \text{ g} \times 0.79 \text{ J/g}\cdot^\circ\text{C} \times \Delta T + 111.7 \text{ g} \times 0.45 \text{ J/g}\cdot^\circ\text{C} \times \Delta T$
 $850.5 \times 10^3 = (80.58 + 50.27) \Delta T = 130.9 \Delta T$
 $\Delta T = 850.5 \times 10^3 / 130.9 = 6.5 \times 10^3^\circ\text{C}$
 Final temperature = $(25 + 6.5 \times 10^3)^\circ\text{C} = 6.5 \times 10^3^\circ\text{C}$
 (only approximate; see below)
- (c) The final temperature is well above the melting point of iron and hence we would expect the iron to melt. However, we should calculate if, after reaching 1535°C (the mp of Fe), there is enough heat (270 J/g) to melt the Fe.
 let $T_{\text{final}} = 1535^\circ\text{C}$ then $\Delta T = (1535 - 25)^\circ\text{C} = 1510^\circ\text{C}$
 $Q = (102 \times 0.79 \times 1510) + (111.7 \times 0.45 \times 1510) = 200 \times 10^3 \text{ J}$
 hence there are $(850.5 - 200) \times 10^3 \text{ J} = 650.5 \times 10^3 \text{ J}$ still available to melt the Fe.
 heat to melt 111.7 g Fe = $111.7 \text{ g} \times 270 \text{ J/g} = 30 \times 10^3 \text{ J}$
 Therefore there is enough heat to melt the iron and $(650.5 - 30) \times 10^3 \text{ J}$ ($620.5 \times 10^3 \text{ J}$) are left.

We can also calculate if the Al_2O_3 would be melted.

mp of $\text{Al}_2\text{O}_3 = 2072^\circ\text{C}$; heat of fusion of $\text{Al}_2\text{O}_3 = 1071 \text{ J/g}$

Assuming that molten Fe has the same specific heat as solid Fe, we can calculate the amount of additional heat needed to reach the melting point of Al_2O_3 .

$$\Delta T = 2072 - 1535 = 537^\circ\text{C}$$

$$Q = [(102 \times 0.79 \times 537) + (111.7 \times 0.45 \times 537)] \text{ J}$$

$$= 70 \times 10^3 \text{ J}$$

Hence, after reaching 2072°C , $(620 - 70) \times 10^3 = 550 \times 10^3 \text{ J}$ are left.

$$\text{Heat to melt the } 102 \text{ g of } \text{Al}_2\text{O}_3 = 102 \text{ g} \times 1071 \text{ J/g} = 109 \times 10^3 \text{ J}$$

$$\text{Heat left} = (550 - 109) \times 10^3 \text{ J} = 441 \times 10^3 \text{ J}$$

Again, assuming molten Al_2O_3 has the same specific heat as the liquid, we can calculate the approximate final temperature.

$$441 \times 10^3 \text{ J} = (102 \times 0.79 \times \Delta T) + (111.7 \times 0.45 \times \Delta T)$$

$$\Delta T = 441000 / 130.9 = 3370^\circ\text{C}$$

$$\text{Final temperature} = 3370 + 2072 = 5442^\circ\text{C} (5.4 \times 10^3^\circ\text{C})$$

When this reaction used to be used for welding rails, it would have been done in the open and much of the heat would have been lost and maybe the Al_2O_3 would not have melted.